

Practice Test 3

MAT0024

Evaluate: exponent 2

1) $\rightarrow 3^2 = -3 \cdot 3 = \boxed{-9}$

Opposite
value of
the product

base 3

exp. 2

2) $(-2)^3 = (-2)(-2)(-2)$

base -2

exp. 3

$= \boxed{-8}$

3) $2 \cdot x \cdot y^2$ for $x=2$ and $y=-3$

$2 \cdot (2) \cdot (-3)^2$

$2 \cdot (2) \cdot (-3)(-3)$

$4 \cdot 9$

$\boxed{36}$

Simplify each expression. Write the answers without parentheses or negative exponents.

$$\begin{aligned}
 (4) \quad (5^1 x^1 y^4)^3 &= 5^{1 \cdot 3} x^{1 \cdot 3} y^{4 \cdot 3} \\
 &= 5^3 x^3 y^{12} \\
 &= \underset{\downarrow}{5} \cdot \underset{\downarrow}{5} \cdot \underset{\downarrow}{5} \cdot x^3 y^{12} \\
 &= \boxed{125 x^3 y^{12}}
 \end{aligned}$$

$$\begin{aligned}
 (5) \quad (-3x)(8x^3) &= (-3)(8) \cdot x^1 \cdot x^3 \\
 &= \boxed{-24x^4}
 \end{aligned}$$

$$(6) \quad \underbrace{(2x^4y^3)}_{\text{Base}}^0 \xleftarrow{\text{exponent}} = 1 \quad * \text{ any base raised to a zero power equals 1.}$$

$$\begin{aligned}
 (7) \quad \left(\frac{3x^3}{2b^4} \right)^{-4} &= \frac{3^{1 \cdot -4} x^{3 \cdot -4}}{2^{1 \cdot -4} b^{4 \cdot -4}} = \frac{3^{-4} x^{-12}}{2^{-4} b^{-16}} \\
 &= \frac{2^4 b^{16}}{3^4 x^{12}} = \boxed{\frac{16 b^{16}}{81 x^{12}}}
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{8} \quad \left(\frac{3a^5}{b^8} \right)^3 &= \frac{3^{1 \cdot 3} a^{5 \cdot 3}}{b^{8 \cdot 3}} \\
 &= \frac{3^3 a^{15}}{b^{24}} \\
 &= \boxed{\frac{27a^{15}}{b^{24}}}
 \end{aligned}$$

$$\textcircled{9} \quad \frac{a^3}{a^{-12}} = a^{12} \cdot a^3 = a^{12+3} = \boxed{a^{15}}$$

$$\begin{aligned}
 \textcircled{10} \quad \frac{56x^4y^2}{7x^2y^9} &= \sqrt[3]{8x^{4-2}y^{2-9}} \\
 &= 8x^2y^{-7} \\
 &= \boxed{\frac{8x^2}{y^7}}
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{11} \quad \frac{x^3y^{-3}a^{-5}}{x^2y^{-4}a^5} &= \frac{x^3y^4}{x^2y^3a^5} \\
 &= \frac{x^{3-2}y^{4-3}}{a^5} \\
 &= \boxed{\frac{xy}{a^5}}
 \end{aligned}$$

(12) $\underbrace{4x^5}_1 - \underbrace{3x^2}_2 \rightarrow \text{binomial}$
 $\rightarrow \text{degree 5}$
 $\rightarrow \text{highest exponent}$

(13) $(\underbrace{3x^2}_1 + \underbrace{7x}_2 + \underbrace{5}_3) + (\underbrace{-8x^2}_1 + \underbrace{-2x}_2 + \underbrace{4}_3)$
 \downarrow
 addition

$$\boxed{-5x^2 + 5x + 1}$$

(14) $(\underbrace{-4x^2}_1 + \underbrace{-3x}_2 + \underbrace{1}_3) - (\underbrace{12x^2}_1 + \underbrace{4x}_2 + \underbrace{3}_3)$
 \downarrow
 subtraction

$$\boxed{-16x^2 - 7x + 4}$$

(15) $3y^3 (-4y^2 + 3y - 6)$

$$\boxed{-12y^5 + 9y^4 - 18y^3}$$

(16) $(\underbrace{5x}_1 - \underbrace{2}_2)(\underbrace{2x}_1 + \underbrace{4}_2) \text{ "FOIL"}$

$$10x^2 + 20x - 4x - 8$$

$$\boxed{10x^2 + 16x - 8}$$

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$$(17) -2x'(5x^2 - 6x' + 3) = \boxed{-10x^3}$$

$$(18) (a' + 5)(a' - 5) = \underset{F}{a^2} - \underset{0}{5a} + \underset{I}{5a} = a^2 + 0 - 25 = \boxed{a^2 - 25}$$

$$(19) (4x + 2)^2 = (4x' + 2)(4x' + 2) = \boxed{16x^2 + 16x + 4}$$

* Poem:

$$\begin{matrix} (4x' + 2)^2 \\ \underset{F}{(4x)}^2 + \underset{L}{2}^2 = (4x)^2 + 16x + 4 \\ = \boxed{16x^2 + 16x + 4} \end{matrix}$$

You Square the first,
Square the last,
multiply them together.
double them both.

$$(20) (y' + 5)(3y^2 - 8y' + 7) = 3y^3 - 8y^2 + 7y + 15y^2 - 40y + 35 = \boxed{3y^3 + 7y^2 - 33y + 35}$$

$$(21) (18y^4 - 24y^2 + 11)(3y^2 - 4y' + 7) = \boxed{54y^6 - 108y^5 + 126y^4 - 72y^4 + 144y^3 - 168y^2 + 117y^2 - 232y + 77}$$

(22) $(2x^2 + 3x - 14) \div (x - 2)$

$$\begin{array}{r} \overline{2x+7} \\ x-2 \overline{) 2x^2+3x-14} \\ \underline{-(2x^2+4x)} \\ 0+7x-14 \end{array}$$

must
add up
to zero!

$$\begin{array}{r} \underline{-(7x+14)} \\ 0+0 \end{array}$$

* remainder

Answer: $\boxed{2x+7}$

① $\frac{2x^2}{x} = 2x$ divide

② $2x(x-2)$ divide
 $2x^2 - 4x$

③ change signs
opposite

④ Add and
bring down
next term

⑤ $\frac{7x}{x} = 7$ divide

⑥ $7(x-2)$ multiply
 $7x - 14$

⑦ $-7x + 14$ change

(23) $\frac{3r^2 + 11r + 7}{r+5}$

$$\begin{array}{r} \overline{3r-4} \\ r+5 \overline{) 3r^2+11r+7} \\ \underline{-(3r^2+15r)} \\ 0-4r+7 \end{array}$$

① $\frac{3r^2}{r} = 3r$ divide

② $3r(r+5)$ multiply
 $3r^2 + 15r$